

Starter Question

The coordinates of two points are $A(3, 4)$ and $B(9, 10)$

Write down the vector \overrightarrow{AB}

What is the magnitude of \overrightarrow{AB} ? Express your answer in the form $p\sqrt{2}$

Write down the unit vector parallel to \overrightarrow{AB}

Is \overrightarrow{AB} parallel to $3\mathbf{i} + 6\mathbf{j}$?
Justify your answer.

Starter Question

a

$$\overrightarrow{AB} = \begin{pmatrix} 6 \\ 6 \end{pmatrix}$$

B1

b

$$\begin{aligned} &\sqrt{6^2 + 6^2} \\ &= \sqrt{72} = 6\sqrt{2} \end{aligned}$$

M1

A1

Just M1 if not simplified

c

$$\frac{1}{6\sqrt{2}} \begin{pmatrix} 6 \\ 6 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

B1

d

No $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ not parallel to $\begin{pmatrix} 1 \\ 2 \end{pmatrix}$

One vector is not a simple multiple of the other

R1

J2

Calculate the magnitude and direction of a vector and convert between component form and magnitude/direction form.

Assessed at AS and A-level

Teaching guidance

Students should be able to answer questions using vectors in two dimensions.

6.2 Components of a vector

Converting Vectors into Component Form

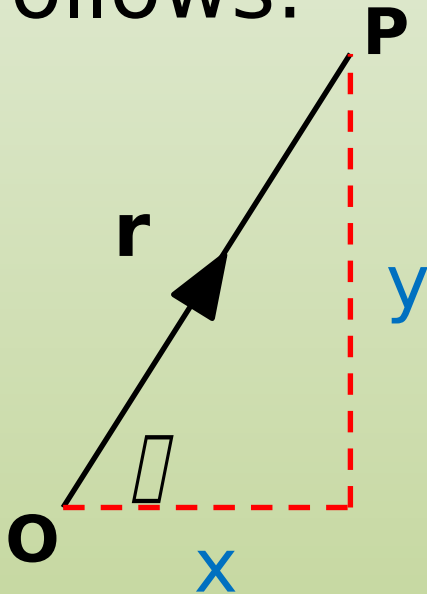
Consider the vector with magnitude and direction to the positive x -axis.

Converting into \mathbf{i} and \mathbf{j} components or a column vector is known as resolving into components.

6.2 Components of a vector

To resolve the vector into component form, we need the values of x and y .

These can be found using basic trig as follows:

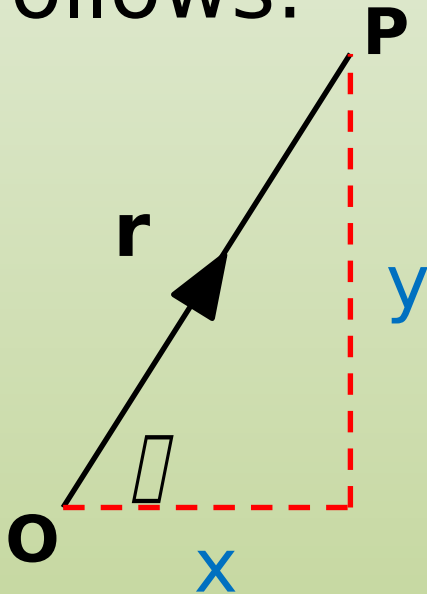


i component (x-value):

6.2 Components of a vector

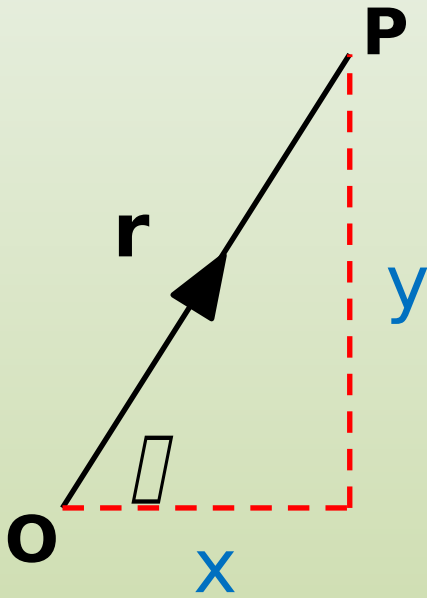
To resolve the vector into component form, we need the values of x and y .

These can be found using basic trig as follows:



j component (y-value):

6.2 Components of a vector

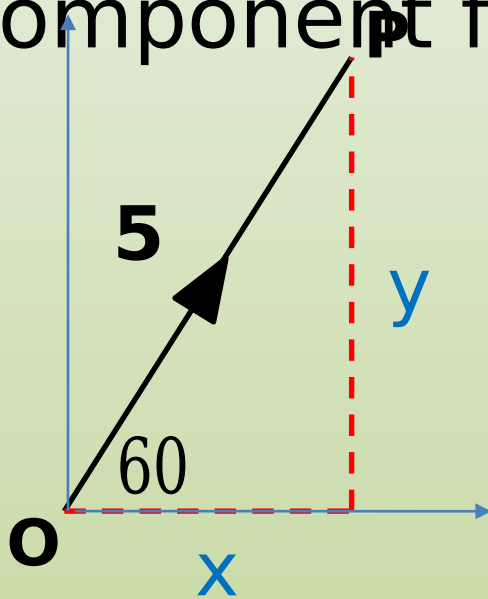


Or

6.2 Components of a vector

Example 1a

Express the following vectors in component form:

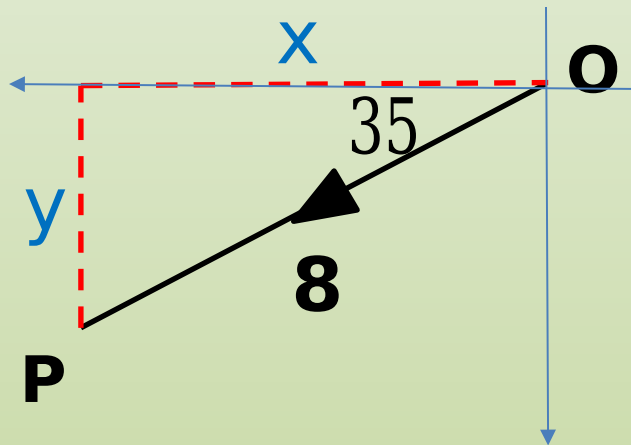


Or

6.2 Components of a vector

Example 1b

Express the following vectors in component form:



Since **x** and **y** are in the negative **i** and **j** directions then:

Or

6.2 Components of a vector

Exercise 6.2A

A cricket ball is hit at ground level on a horizontal surface.

It initially moves at 26 m s^{-1} at an angle of 50° above the horizontal.

- (a) Find the horizontal component of the ball's initial velocity, giving your answer to two significant figures.
- (b) Write down the initial velocity of the ball as a vector in the form $a\mathbf{i} + b\mathbf{j}$

- a) So the horizontal component is 17m/s to 2sf.
- b) $17\mathbf{i} + 20\mathbf{j}$

J4

Understand and use position vectors; calculate the distance between two points represented by position vectors.

Assessed at AS and A-level

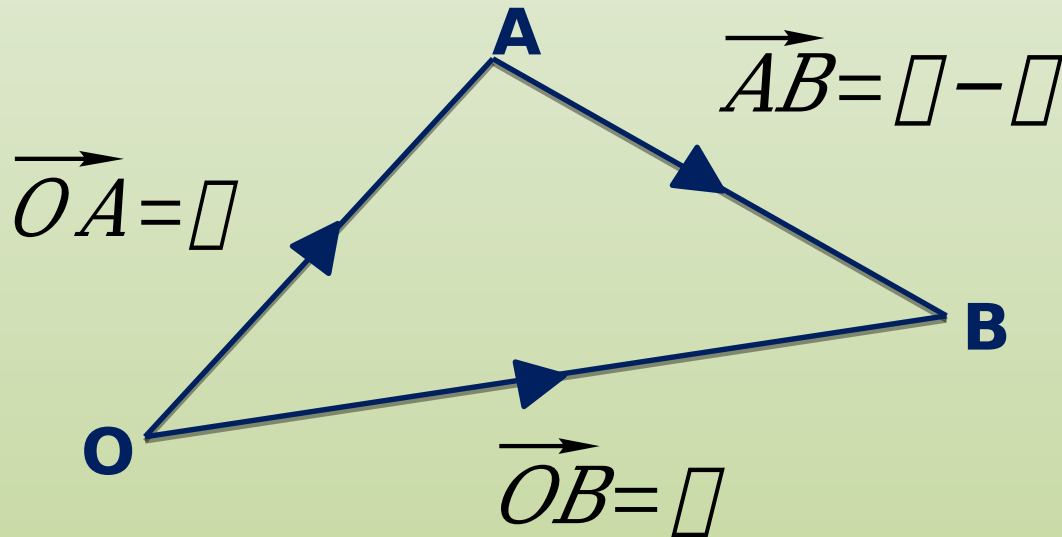
Teaching guidance

Students should be able to:

- understand and use the result $\overrightarrow{AB} = \overrightarrow{OB} - \overrightarrow{OA}$
- use position vectors in both a pure context and in mechanics questions, for example in kinematics.

6.2 Components of a vector

The vector is known as a **direction vector** or a **relative position vector**. That is the position vector of B relative to A.



6.2 Components of a vector

Example 2a

Consider the points with coordinates C(-1, 2) and D(4, -3).

a) Write down the position vectors of points C and D

$$\mathbf{c} = -\mathbf{i} + 2\mathbf{j} \quad \text{OR}$$

$$\mathbf{d} = 4\mathbf{i} - 3\mathbf{j} \quad \text{OR}$$

6.2 Components of a vector

Example 2b

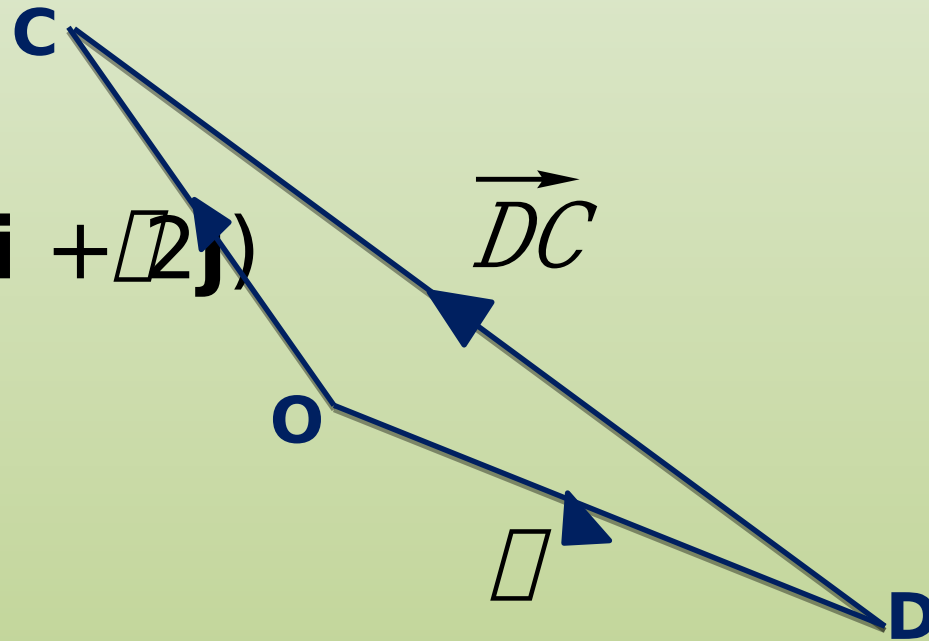
Consider the points with coordinates C(-1, 2) and D(4, -3).

b) Find the direction vector

$$= -\mathbf{d} + \mathbf{c}$$

$$= -(4\mathbf{i} - 3\mathbf{j}) + (-\mathbf{i} + 2\mathbf{j})$$

$$= -5\mathbf{i} + 5\mathbf{j}$$



6.2 Components of a vector

Example 3

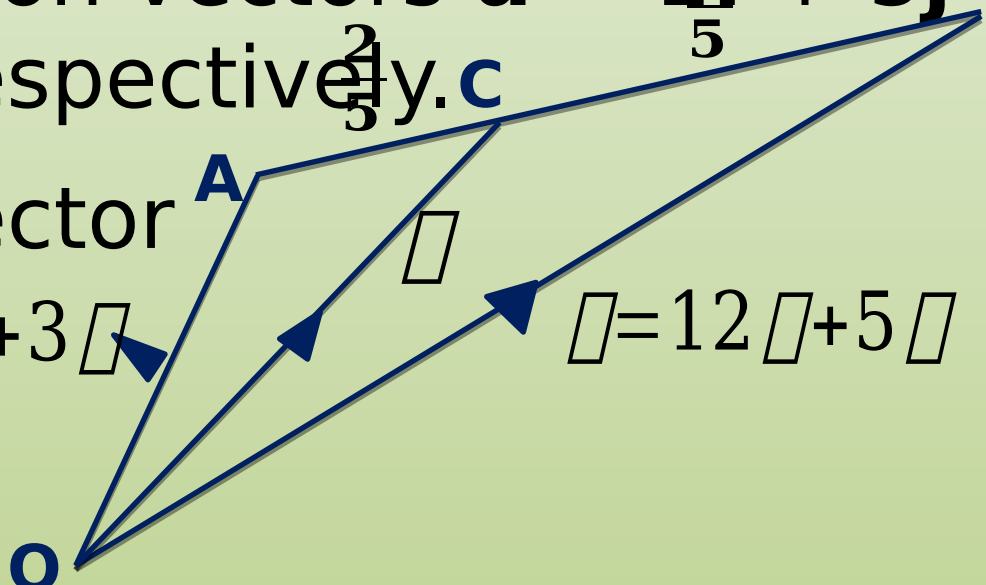
Points A, B and C are collinear, with C between A and B, such that $AC : CB = 2 : 3$.

A and B have position vectors $\mathbf{a} = 2\mathbf{i} + 3\mathbf{j}$ and $\mathbf{b} = 12\mathbf{i} + 5\mathbf{j}$ respectively.

Find the position vector of point C, \mathbf{c} .

$$\vec{OC} = 2\vec{OA} + 3\vec{OB}$$

$$\vec{OC} = 12\vec{e}_1 + 5\vec{e}_2$$



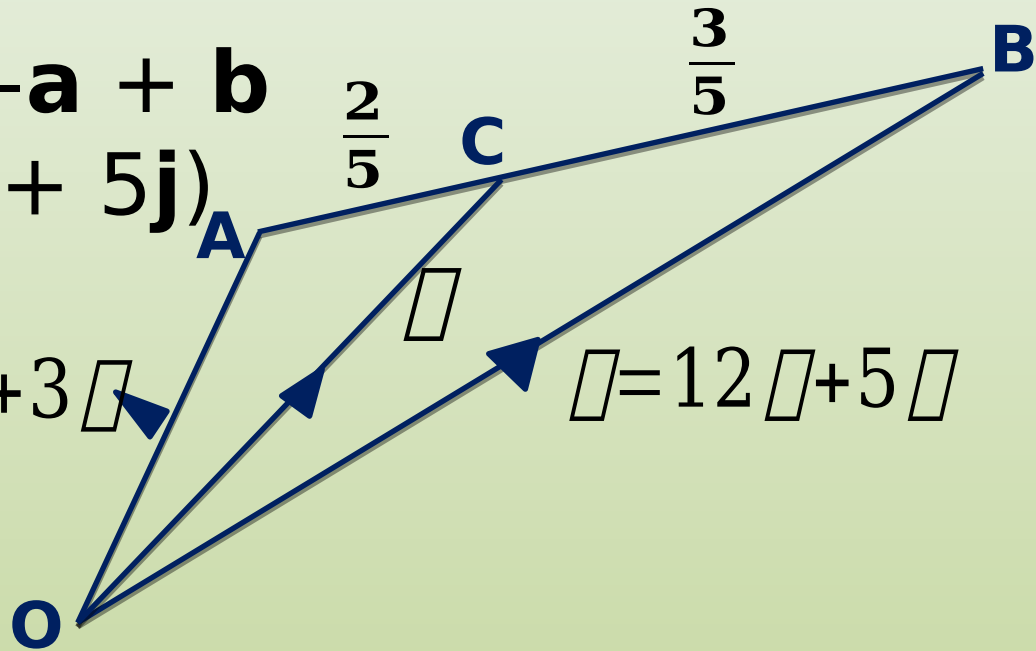
6.2 Components of a vector

Example 3

Find the position vector of point C, **c**.

$$\begin{aligned}\text{Direction vector} &= -\mathbf{a} + \mathbf{b} \\ &= -(2\mathbf{i} + 3\mathbf{j}) + (12\mathbf{i} + 5\mathbf{j}) \\ &= 10\mathbf{i} + 2\mathbf{j}\end{aligned}$$

$$\begin{aligned}\text{Direction vector} &= (10\mathbf{i} + 2\mathbf{j}) \\ &= 4\mathbf{i} + \mathbf{j}\end{aligned}$$



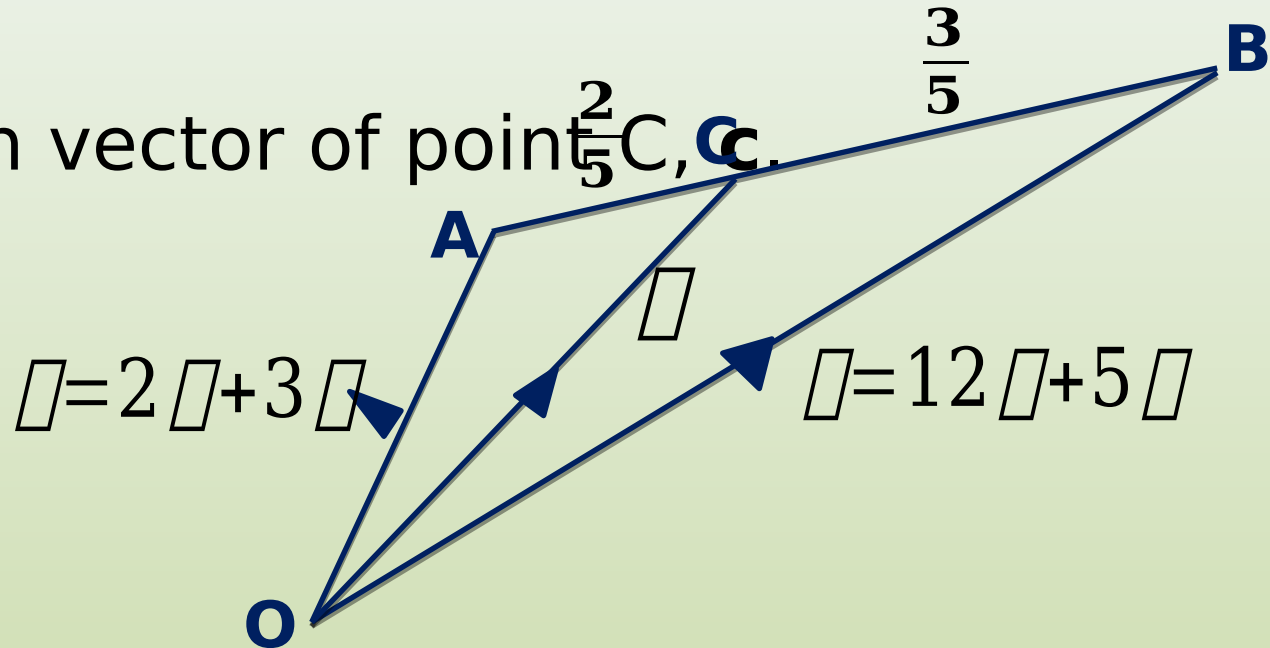
6.2 Components of a vector

Example 3

Find the position vector of point C , \mathbf{c} .

$$= 10\mathbf{i} + 2\mathbf{j}$$

$$= 4\mathbf{i} + \mathbf{j}$$



position vector

$$\mathbf{c} = (2\mathbf{i} + 3\mathbf{j}) + (4\mathbf{i} + \mathbf{j}) = 6\mathbf{i} + 4\mathbf{j}$$

$$\mathbf{c} = 6\mathbf{i} + 3.8\mathbf{j}$$

Exercise

6.2A Q8-